

**FIRST SEMESTER 2023-2024**

**Course Handout Part-II**

In addition to part‑I (General Handout for all courses appended to the timetable), this portion gives further specific details regarding the course.

Course No.: MATH F111

### Course Title: MATHEMATICS I

Instructor‑in‑charge: B. MISHRA

Name of Instructors Sumit Kumar V , Sushil Bhunia, K. Venkata Ratnam, N. Kishore Kumar, Rohit Gupta, Sajith P, Animesh Singh, Purohit Nisarg Bharatbhai, Ameya Kolhatkar, Moreshwar Jagadeorao Tayde, Sayantan Ghosh, Akankshya Sahu, Mintu Mandal, Debarati Mondal, Rabindranath Chakrabortty, Subhendu Paul, Bhawna, Sneha Pradhan, Dhrubajyoti Sarkar, Jahir Abbas Sardar, Md Imadadul Islam, Kailash Chand Swami, Sunil Rampuria, Shayon Bhadra, Shravani Rao

**Scope and Objective of the Course:**

Calculus is needed in every branch of science and engineering, as all dynamics is modeled through differential and integral equations. Functions of several variables appear more frequently in science than functions of a single variable. Their derivatives are more interesting because of the different approaches in which the variables can interact. Their integrals occur in several areas. All these lead in a natural way to functions of several variables.

**Text Book:**

1. George B. Thomas, Maurice D. Weir and Joel Hass, *Thomas*’ *Calculus*, Pearson, 14th Edition, 2018.

**Reference Books:**

1. Erwin Kreyszig, *Advanced Engineering Mathematics*, 10th Edition, Wiley-India, 2015.
2. James Stewart, *Calculus*, 7th Edition, Cengage Learning, 2017.
3. Monty J. Strauss, Gerald L. Bradley and Karl J. Smith, *Calculus*, 3rd Edition, Pearson, 2007.

**Course Plan:**

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| --- | --- | --- | --- |
| **Lect. No.** | **Learning Objectives** | **Topics to be Covered** | **Chapter in the Text Book** |
| 1 | Overview of the course | **-** | **-** |
| 2-3 | To explain how calculus of one variable real-valued functions are related to vector valued functions. | Limit, continuity and differentiability of vector functions, arc length, velocity and unit tangent vector | 13.1, 13.2 (only Integrals of Vector Functions is included, Projectile Motion is excluded), 13.3 |
| 4-6 | To explain the concepts of curvature and torsion. | Curvature, normal vector, torsion and binormal vector, tangential and normal components of velocity and acceleration | 13.4, 13.5 |
| 7-8 | To learn to prove continuity, discontinuity and existence of limits for the functions of several variables. | Functions of several variables, level curves, limits, continuity | 14.1, 14.2 |
| 9-11 | To define partial derivatives and explain the chain rules for functions of several variables | Partial derivatives, chain rule | 14.3, 14.4 |
| 12-14 | To explain how to find the derivative along a particular direction | Directional derivative, gradient vectors, tangent planes and normal line, Estimating the change in a specific direction, Linearization of functions of two and three variables, The error in the standard linear approximation | 14.5, 14.6 |
| 15-17 | To explain the concepts of local maximum and minimum for functions of several variables | Maximum, minimum and saddle points of functions of two or three variables, constrained maxima and minima – method of Lagrange multipliers. | 14.7, 14.8 |
| 18-20 | How to obtain length of a polar curve and area of a surface of revolution of a polar curve? | Polar Coordinates, Graphing in Polar Coordinates, Length of a polar curve, Conics in polar coordinates. | 11.3-11.5 and 11.7 |
| 21-22 | How formula for area in polar coordinates can be found through polar double integral? | Double integrals, area, change of integrals to polar coordinates. Double integrals in polar form | 15.1 - 15.4 |
| 23-26 | To identify which type of integral evaluates volume of a solid in a simpler way | Triple integral, integral in Cylindrical and Spherical coordinates, Substitutions in multiple integrals | 15.5, 15.7, 15.8 |
| 27-31 | To explain the equivalent definitions of conservative field and understand how Green’s theorem can simplify evaluation of line integrals. | Line integral, work, circulation, flux, path independence, potential function, conservative fields, Green’s theorem in the plane | 16.1 – 16.4 |
| 32-35 | To explain the concept of surface measure and learn to apply Stokes theorem | Surface area and surface integral, Stokes’ theorem, Gauss divergence theorem | 16.5 - 16.8 |
| 36-40 | To explain the convergence of infinite series with examples and counter examples | Sequence of real numbers, frequently occurring limits.  Infinite series, different tests of convergence, series of nonnegative terms, absolute and conditional convergence, alternating series. | 10.1 – 10.2 ***(self-study)***  10.3-10.6 |
| To explain the power series and their properties | Power series, Taylor and Maclaurin series | 10.7 – 10.8 |

**Evaluation Scheme:**

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| --- | --- | --- | --- | --- | --- |
| **EC No.** | **Evaluation Component** | **Duration** | **Weightage\*** | **Date & Time** | **Nature of Component** |
| 1. | Quiz - I | --- | 12.5 | TBA | Closed Book |
| 2. | Mid-Sem. | 90 minutes | 30 | TBA | Closed Book |
| 3. | Quiz - II | --- | 12.5 | TBA | Closed Book |
| 4. | Comprehensive Examination | 3 hours | 22.5  22.5 | TBA | Closed Book  Open Book |

**\* The total marks of all the components, taken together will be 200**.

**Chamber consultation hour:** To be announced in the class.

**Make-up Policy**:

Make-up will be given only for very genuine cases and prior permission has to be obtained from the I/C.

**Notices:** The notices concerning this course will be displayed on the CMS Notice Board only.

**Academic Honesty and Integrity Policy:** Academic honesty and integrity are to be maintained by all the students throughout the semester and no type of academic dishonesty is acceptable.

**INSTRUCTOR IN ‑CHARGE**

**MATH F111**